Convergence Analysis of a Momentum Algorithm with Adaptive Step Size for Nonconvex Optimization

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A Momentum Algorithm with Adaptive Step Size

- ▶ ADAM famous **BUT** convergence issues (Reddi et al., 2018).
- Several variants : Yogi, AdaBound, AdaShift, Nadam, QHAdam, RAdam ...
- ► **Goal**: convergence rates for adaptive algorithms (ADAM in particular) for **nonconvex** optimization.

Algorithm

$$\begin{cases} x_{n+1} = x_n - a_{n+1}p_{n+1} \\ p_{n+1} = p_n + b\left(\nabla f(x_n) - p_n\right) \end{cases}$$

where $a_n \in \mathbb{R}^d_+$ $b \ge 0$, $x_0, p_0 \in \mathbb{R}^d$.

Contributions

Main Idea

Clipping the effective step size a_{n+1} :

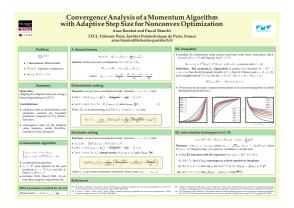
$$0 < \delta \le a_{n+1} \le a_{sup}(L) \tag{1}$$

Results

- ▶ O(1/n) convergence rate for ADAM in deterministic and stochastic settings. (control of $\min_{0 \le k \le n-1} \|\nabla f(x_k)\|^2$).
- Convergence rate analysis of the objective function using the Kurdyka-Łojasiewicz (KŁ) property.

Thank you for your attention

Feel free to come to my poster



For more details: article available on the Workshop page / arXiv.

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